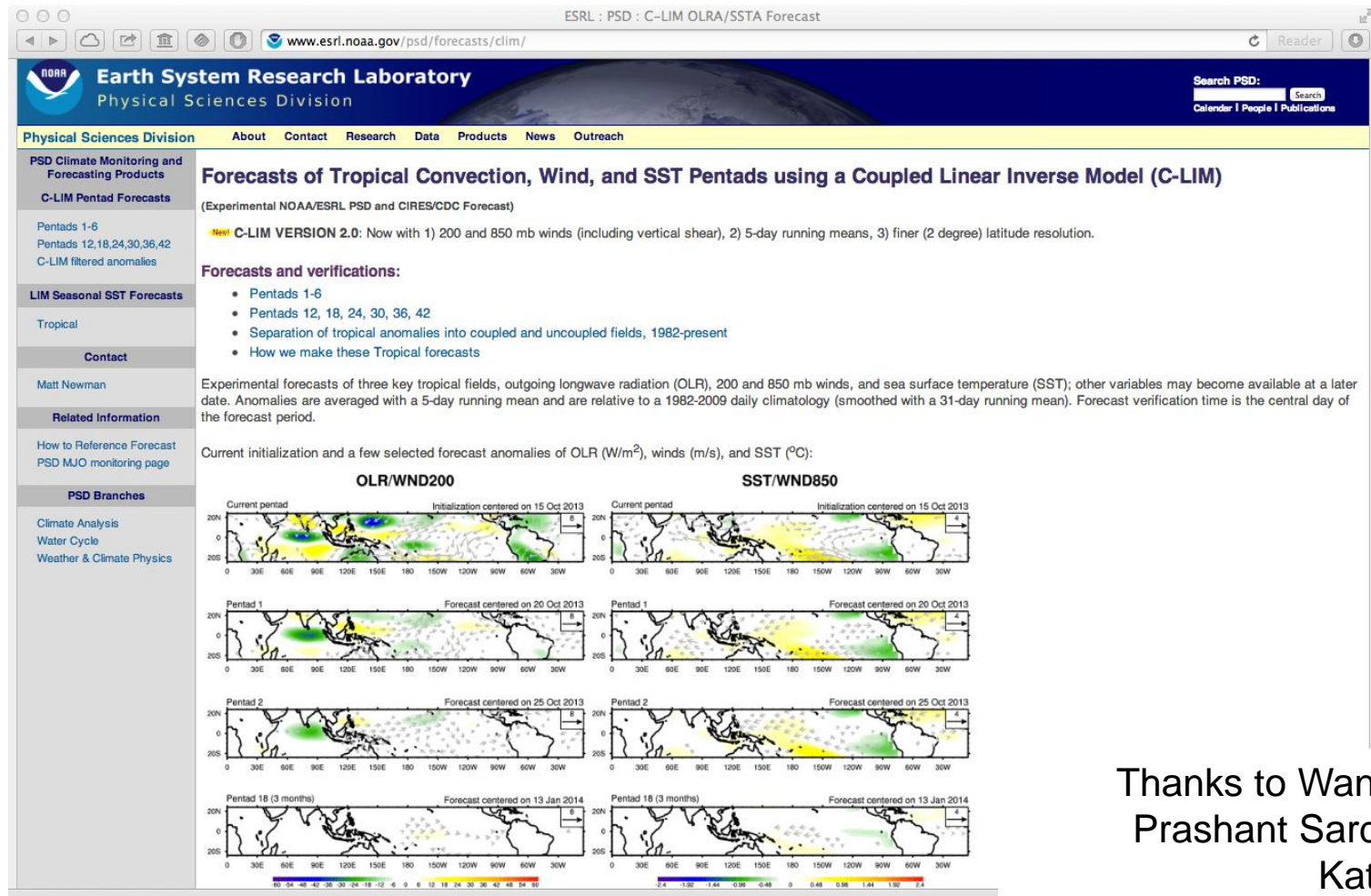


Diagnosing subseasonal predictability of tropical atmospheric anomalies

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Thanks to Wanqiu Wang,
Prashant Sardeshmukh,
Kathy Pegen

“Multivariate Red Noise” null hypothesis

$$d\mathbf{x}/dt = \mathbf{L}\mathbf{x} + \mathbf{F}_s$$

$\mathbf{x}(t)$ is a series of maps, \mathbf{L} is stable, and \mathbf{F}_s is white noise (maps)

- Determine \mathbf{L} and \mathbf{F}_s using “Linear Inverse Model” (LIM)
 - \mathbf{x} is **SST/OLR/200 and 850 mb wind** 5-day running mean anomalies in Tropics, 1982-2009 (similar to Newman, Sardeshmukh, and Penland 2009, *J. Climate*)
 - prefiltered in reduced EOF space
 - LIM determined from specified lag $\tau_0=5$ (e.g., the data averaging interval) as in AR1 model, using τ_0 - and zero-lag covariance of \mathbf{x}
 - Test the LIM over much longer time intervals: observed spatio-temporal lag-covariance statistics very well reproduced
 - Hindcasts determined from cross-validation (10% data withheld to recompute \mathbf{L})

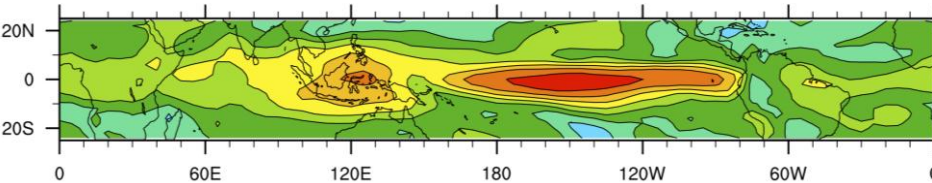
LIM has skill comparable to CFS2

OLR forecast skill, 1982-2009

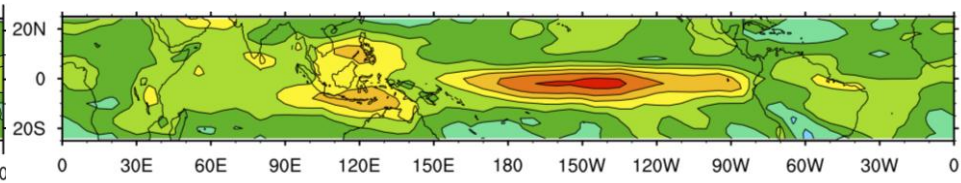
LIM

CFS2

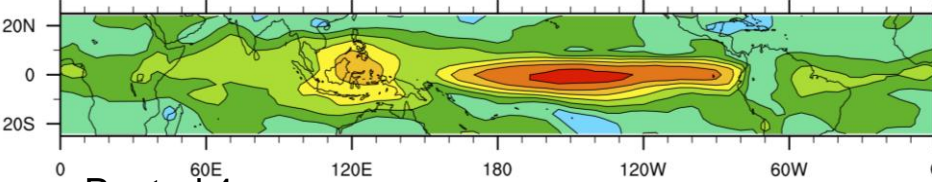
Pentad 2



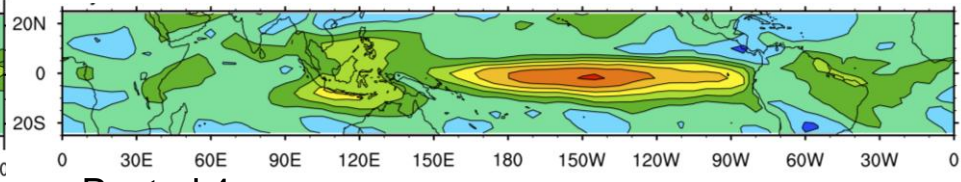
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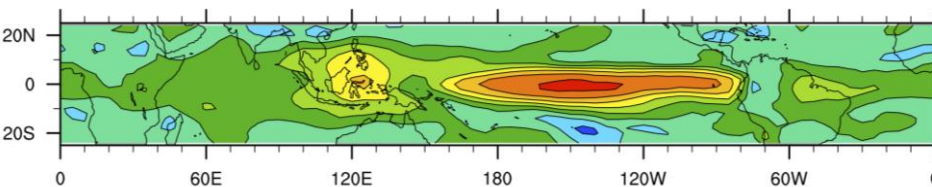
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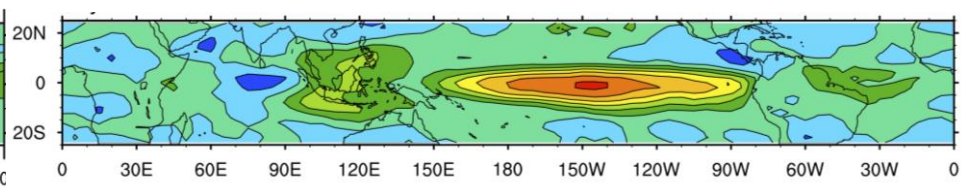
Pentad 3



Pentad 4



Pentad 4



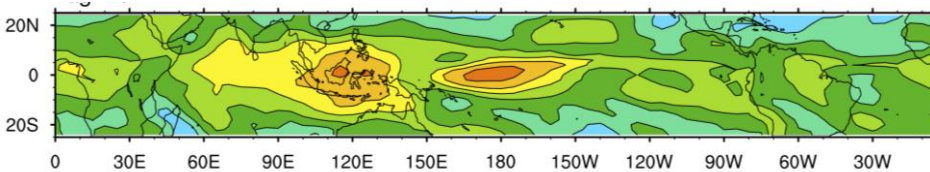
LIM has skill comparable to CFS2

OLR forecast skill, 1999-2009

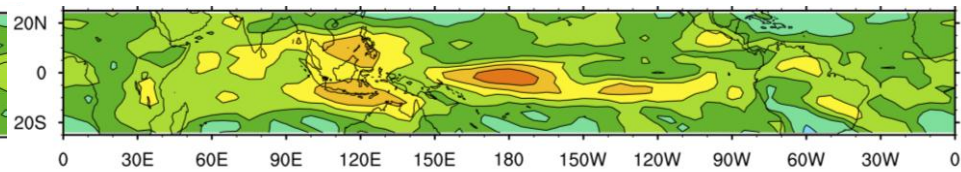
LIM

CFS2

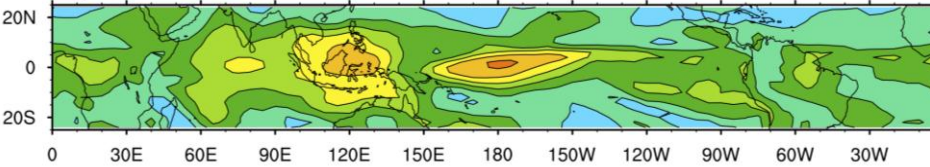
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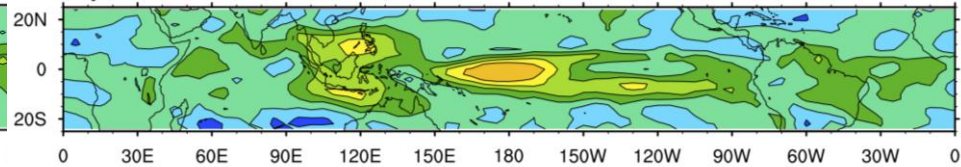
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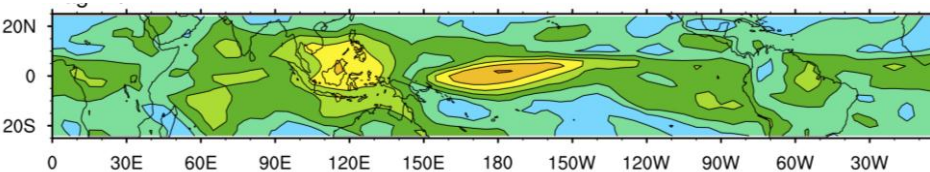
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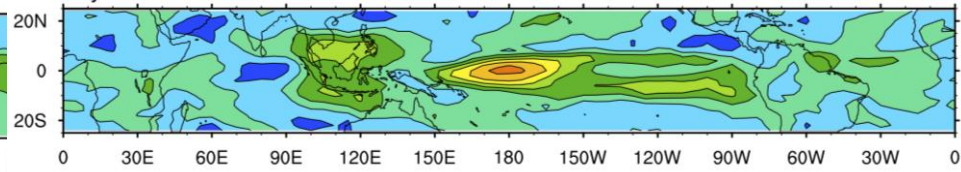
Pentad 3



Pentad 4



Pentad 4



Using LIM to estimate predictability

$$d\mathbf{x}/dt = \mathbf{L}\mathbf{x} + \mathbf{F}_s$$

\mathbf{L} = constant, \mathbf{F}_s = additive (state-independent) noise.

$$\mathbf{x}(t + \tau) = \exp(\mathbf{L}\tau) \mathbf{x}(t) + \boldsymbol{\varepsilon} = \mathbf{G}(\tau) \mathbf{x}(t) + \boldsymbol{\varepsilon}$$

“signal”

“noise”

Expected forecast error covariance

(assuming no initial error) :

$$\mathbf{E}(\tau) = \langle \boldsymbol{\varepsilon} \boldsymbol{\varepsilon}^T \rangle = \mathbf{C}(0) - \mathbf{G} \mathbf{C}(0) \mathbf{G}^T$$

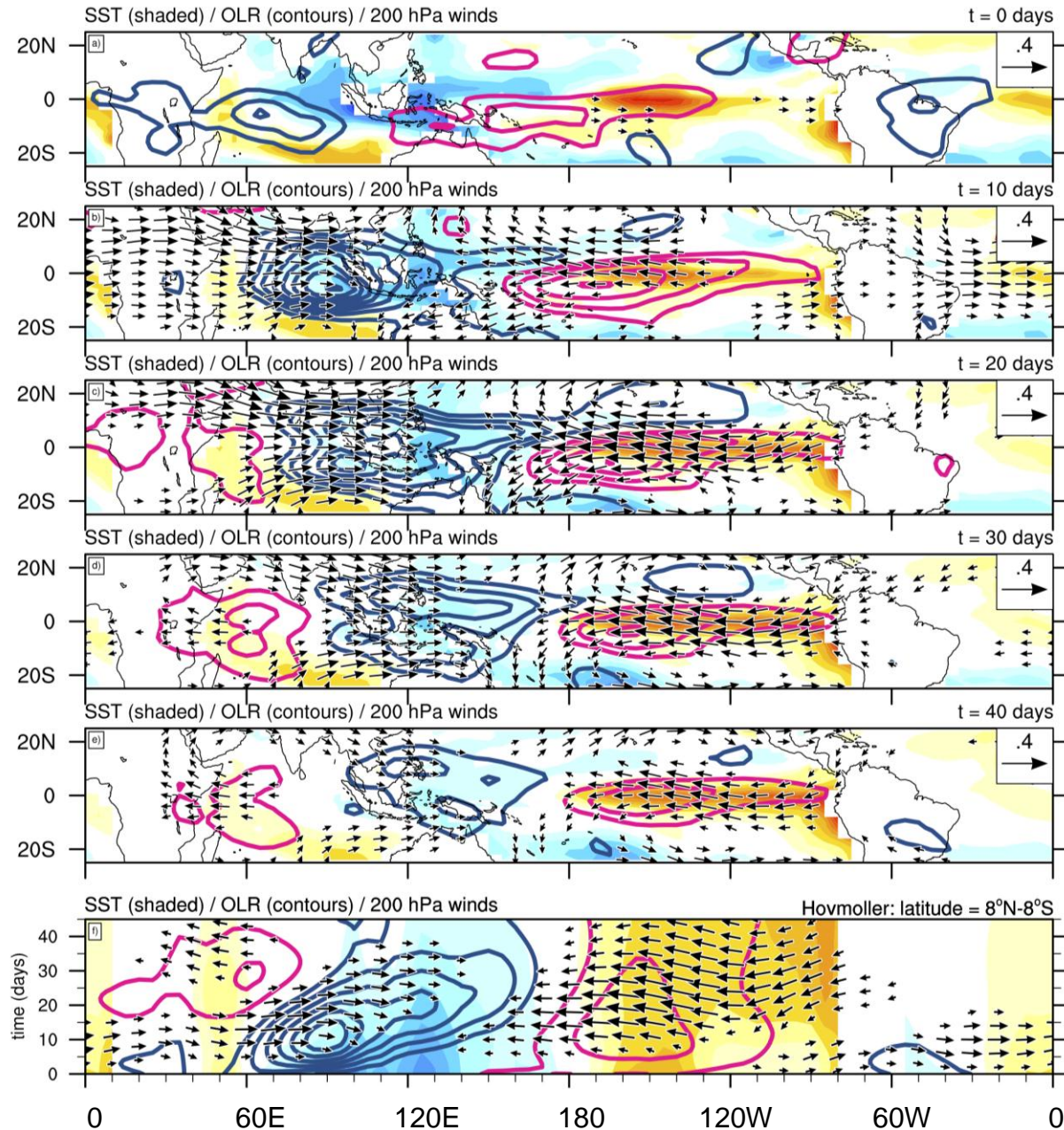
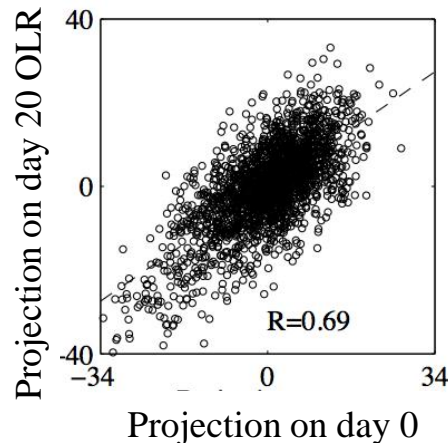
Expected forecast anomaly correlation

$$\rho_\infty = \frac{s}{\sqrt{1+s^2}}, \text{ where } s^2 = \frac{[\mathbf{G} \mathbf{C}(0) \mathbf{G}^T]_{ii}}{[\mathbf{E}(\tau)]_{ii}}$$

Larger signal related to leading singular vector of $\mathbf{G}(\tau)$

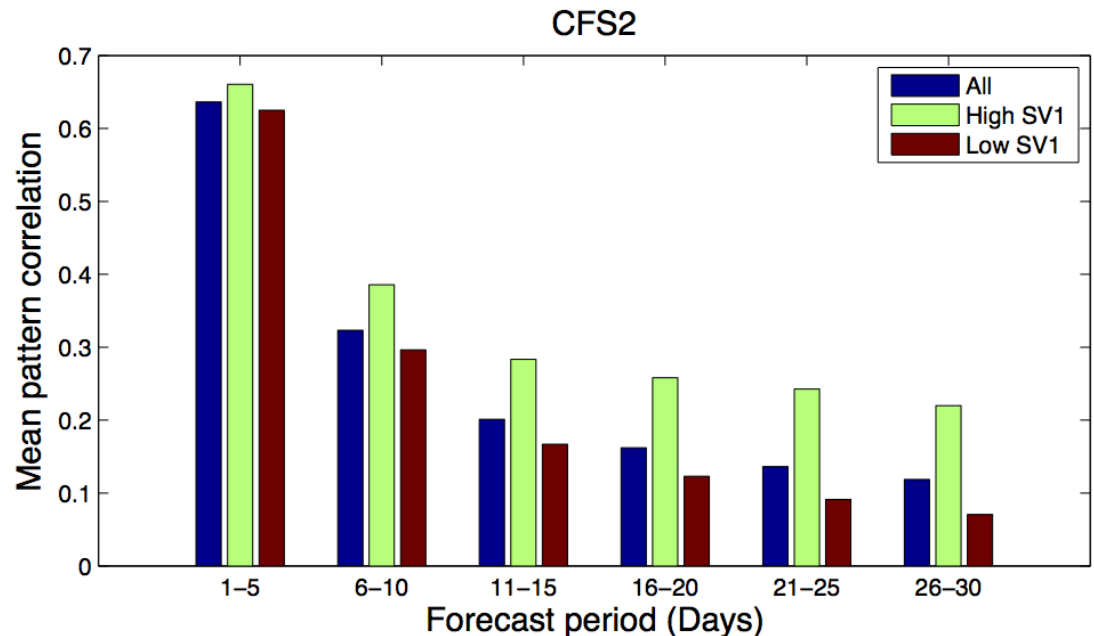
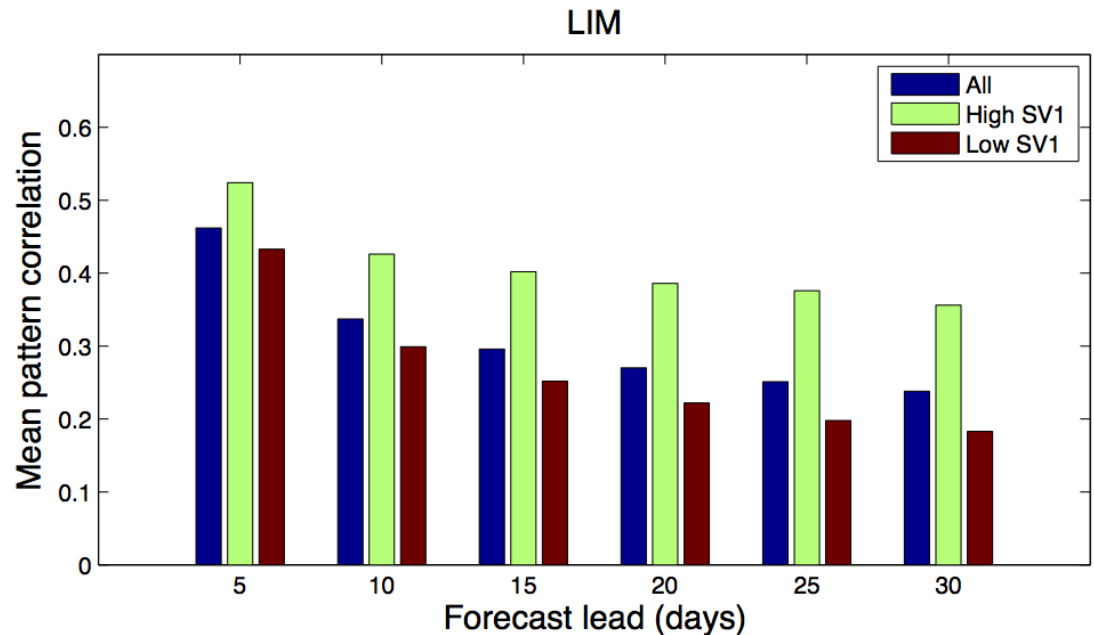
“Optimal” structure
leading to greatest
tropical OLR
anomaly growth
over 20 days

Shading: SST
Contours: OLR
Vectors: 200 mb winds



Using LIM to identify relatively more skillful forecast cases *a priori* from forecast signal-to-noise ratio

*Pattern correlation of tropical IndoPacific OLR hindcasts, 1982-2009, stratified by whether initial conditions **do** or **do not** strongly project on initial growth structure (SV1)*



Two distinct eigenmode spaces in L

“coupled”

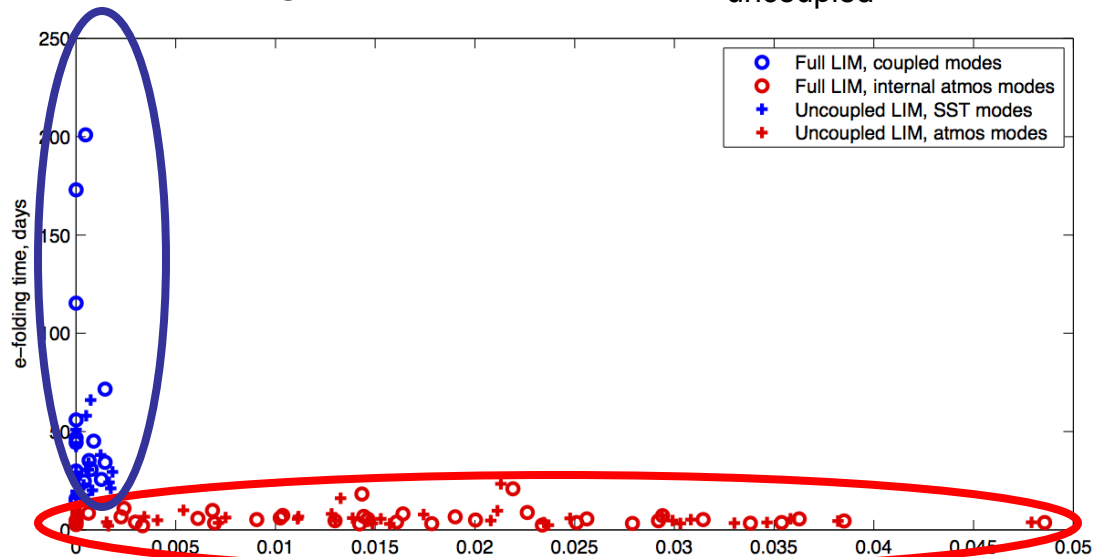
Longer e-folding time, low frequency modes strongly modified by coupling within L

“internal atmospheric”

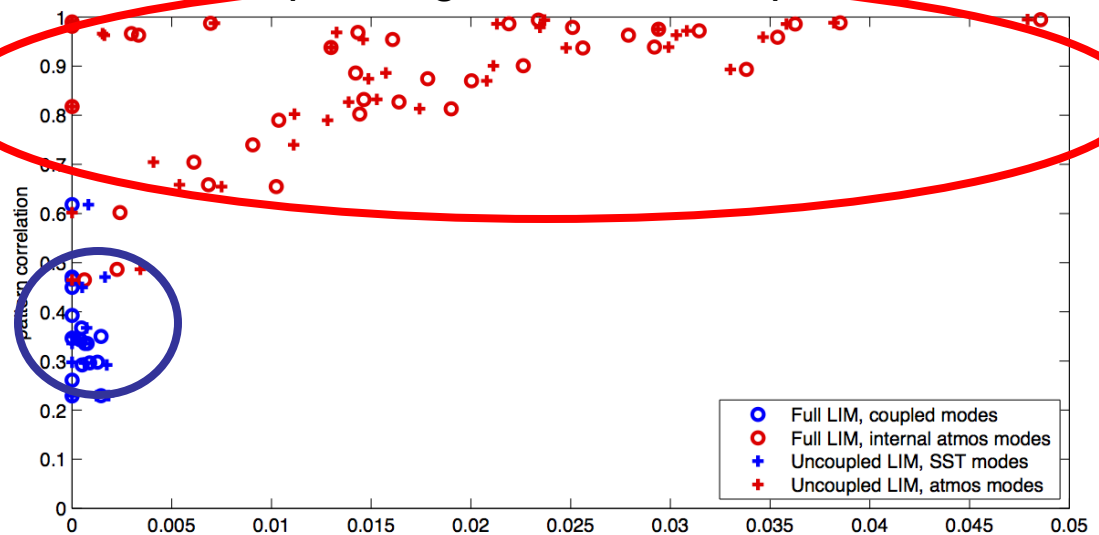
Short e-folding time, high frequency modes only slightly modified by coupling within L

(Newman et al. 2009)

Eigenvalues of L and $L_{\text{uncoupled}}$



Maximum pattern correlation between corresponding full and uncoupled modes



Frequency (days⁻¹)

Project tropical state vector \mathbf{x} into “coupled” and “internal” subspaces of full operator \mathbf{L}

Define

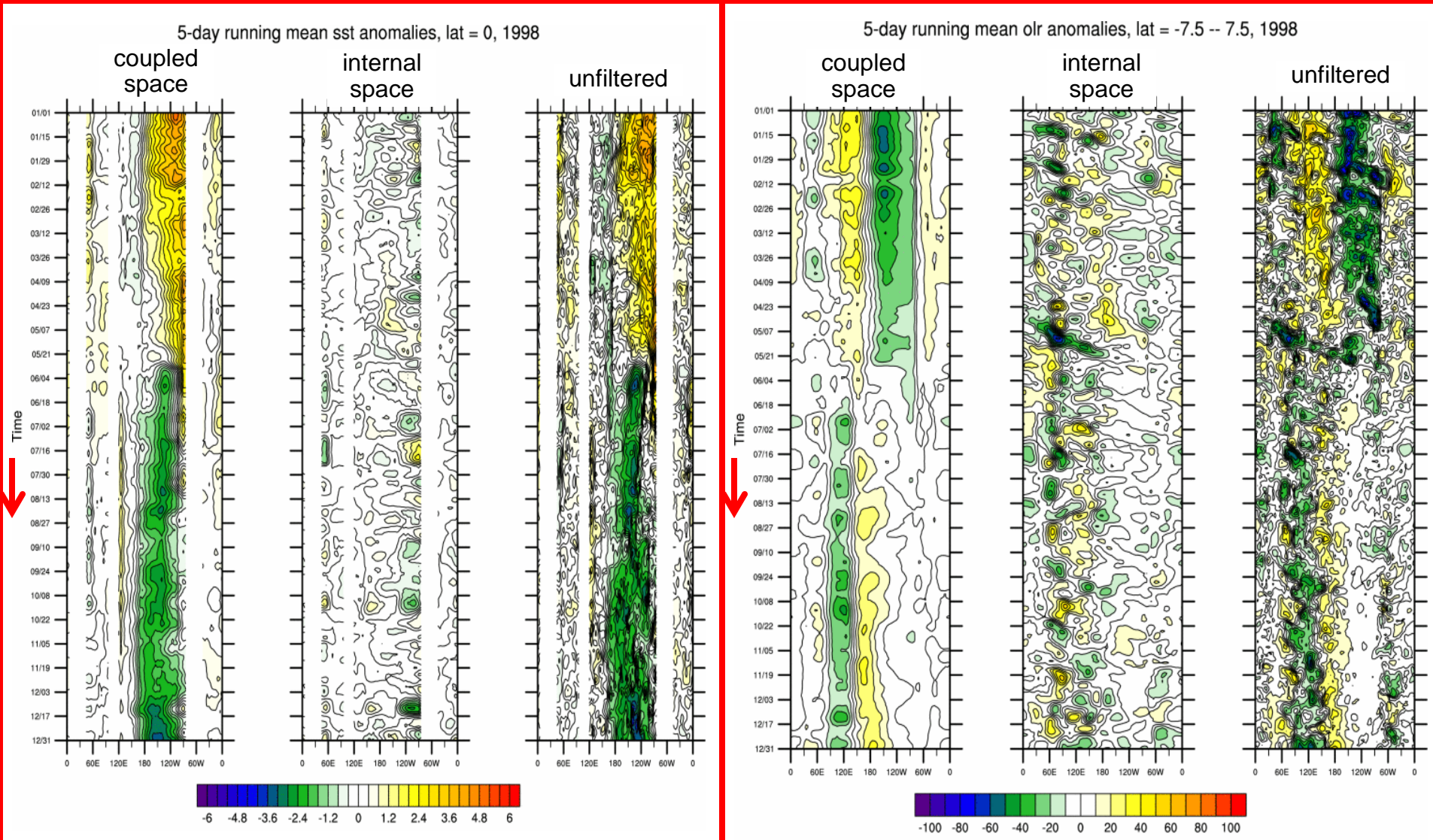
$$\mathbf{x} = \mathbf{x}^{\text{coup}} + \mathbf{x}^{\text{int}}$$

where

$$\mathbf{x}^{\text{coup}} = \sum_j \mathbf{u}_j^{\text{coup}} \alpha_j^{\text{coup}}(t) \quad \mathbf{x}^{\text{int}} = \sum_j \mathbf{u}_j^{\text{int}} \alpha_j^{\text{int}}(t)$$

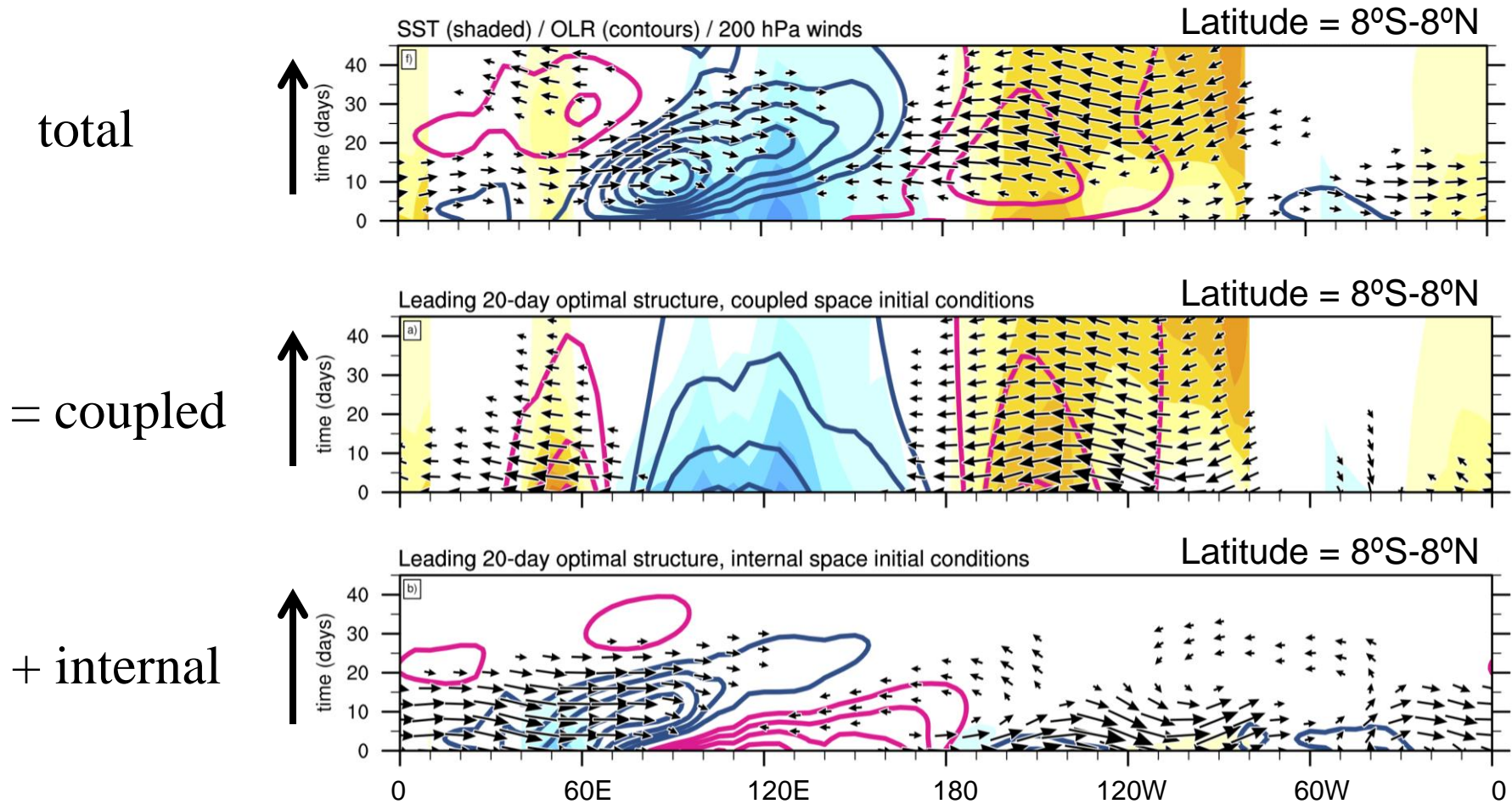
Note: \mathbf{x}^{coup} and \mathbf{x}^{int} need not be orthogonal

Using the LIM to “filter” the data



1. no temporal filter is applied
2. interannual variability defined dynamically

Optimal structure for 20-day OLR anomaly growth, decomposed into coupled and internal spaces



Maximum growth: coupled and internal spaces evolve from destructive to constructive interference

Shading: SST
Contours: OLR
Vectors: 200 mb winds

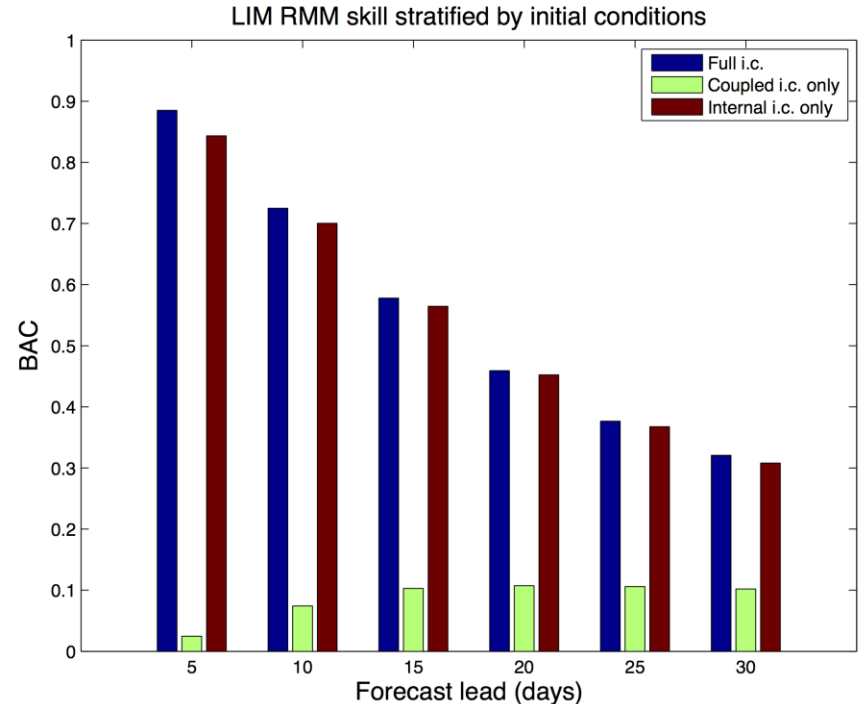
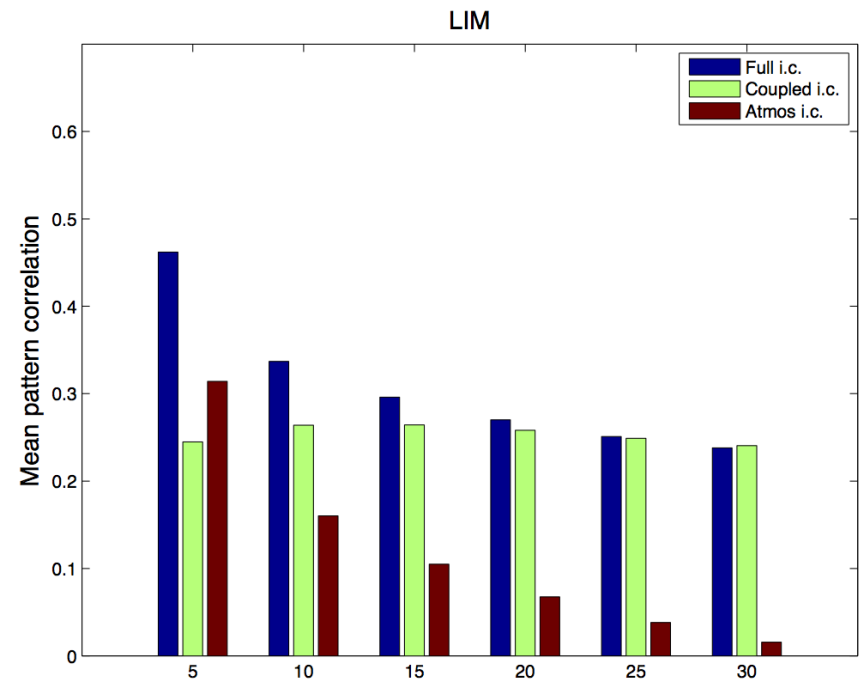
Most LIM skill due to coupled space initial conditions for leads > 15 days

Pattern correlation of tropical IndoPacific OLR LIM hindcasts, 1982-2009, where forecast initial conditions are either:

Full

Coupled space only

Internal space only



Conclusions

- LIM useful for diagnosis of predictability, **because** its forecast skill is comparable with coupled GCMs and it reproduces observed spatio-temporal statistics
- In Tropics, two nonorthogonal linear dynamical systems:
 - Slow (~interannual) coupled space **more predictable even for relatively “short” leads**
 - Fast (~intraseasonal) internal atmosphere space **less predictable, although MJO in this space**
 - Projecting data onto coupled space acts as an effective “filter”; MJO indices may convolve dynamics
- Subseasonal forecast skill may itself be *predicted* based on LIM signal-to-noise
 - In LIM, there is no “spread/skill” relationship, but note this need not be a constraint for all linearly predictable systems
 - Plan to institute “forecasts of forecast skill” in LIM forecast web page <http://www.esrl.noaa.gov/psd/forecasts/clim/>

Bivariate correlation (CORR) and RMSE for PC1 and PC2

i. Definition of Intraseasonal anomaly

$$F' = F - F_c - F_L$$

F : Total field

F_c : Daily climatology

F_L : Previous 90-day average of $F - F_c$

ii. Target period for calculating CORR and RMSE

9May1999 - 31Dec2009

iii. Calculation of PCs

- Base EOFs were computed with combined fields NOAA OLR and CFSR U200/ U850 (15S-15N average and 20-90-day filtered) (Wang et al. 2013.)
- F' of pentad average from CFSv2, CLIM, and observations (NOAA OLR, and R1 U200/U850) are projected onto the base EOFs
- The resulting PCs are normalized by the standard deviation of the PCs of the observation

